



Overview of post-quantum cryptography

CSE 539

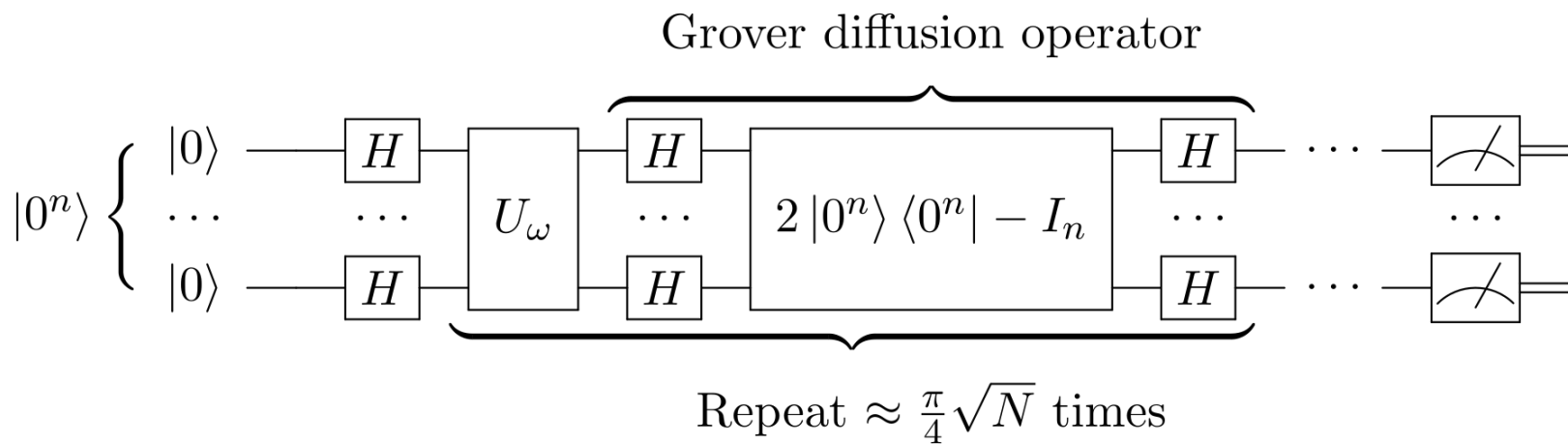
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What we need

- Symmetric
 - Encryption
 - Authentication
 - Secure hashes
 - Others?
- Asymmetric
 - Encryption
 - Non-repudiability (signatures)
 - Key exchange
 - Others? (e.g., homomorphic)

Grover's algorithm



https://en.wikipedia.org/wiki/Grover%27s_algorithm#/media/File:Grover's_algorithm_circuit.svg



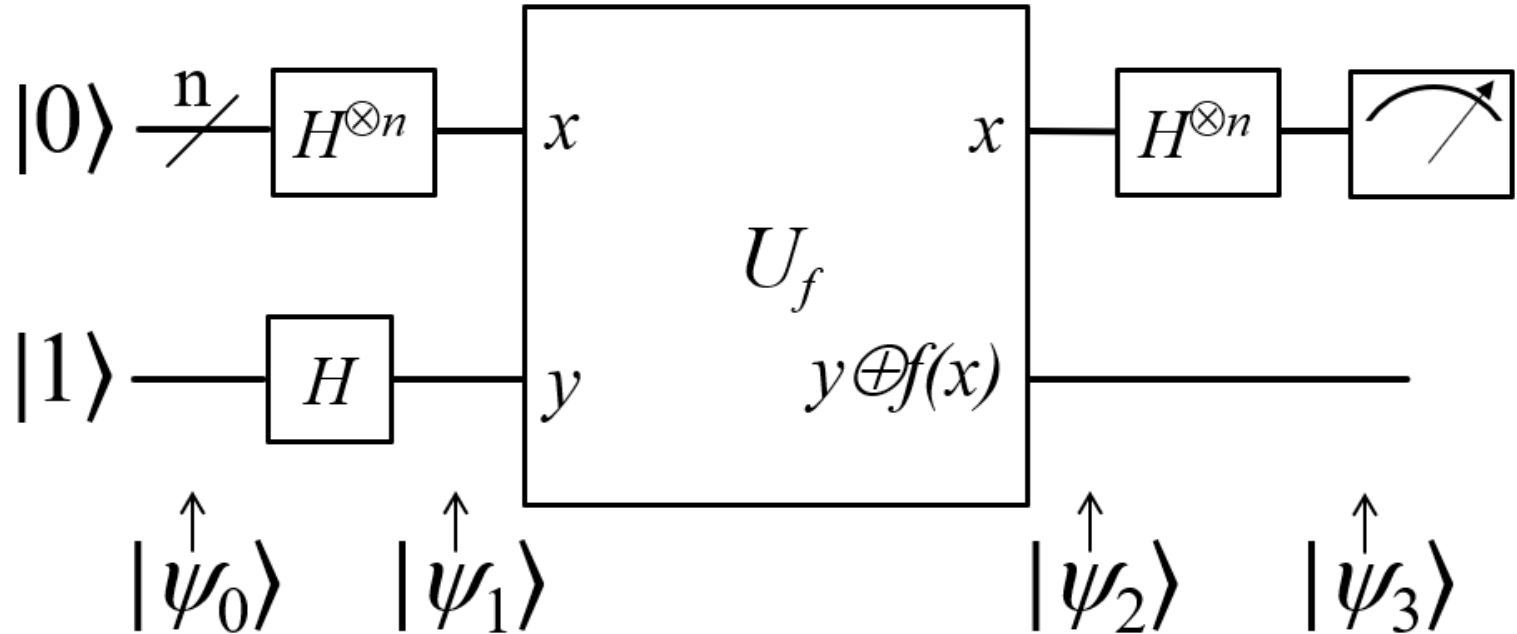
Symmetric crypto

- Double the key size
 - $\text{sqrt}(2^{2n}) = 2^n$
 - $\text{sqrt}(2^{256}) = 2^{128}$

Asymmetric Crypto

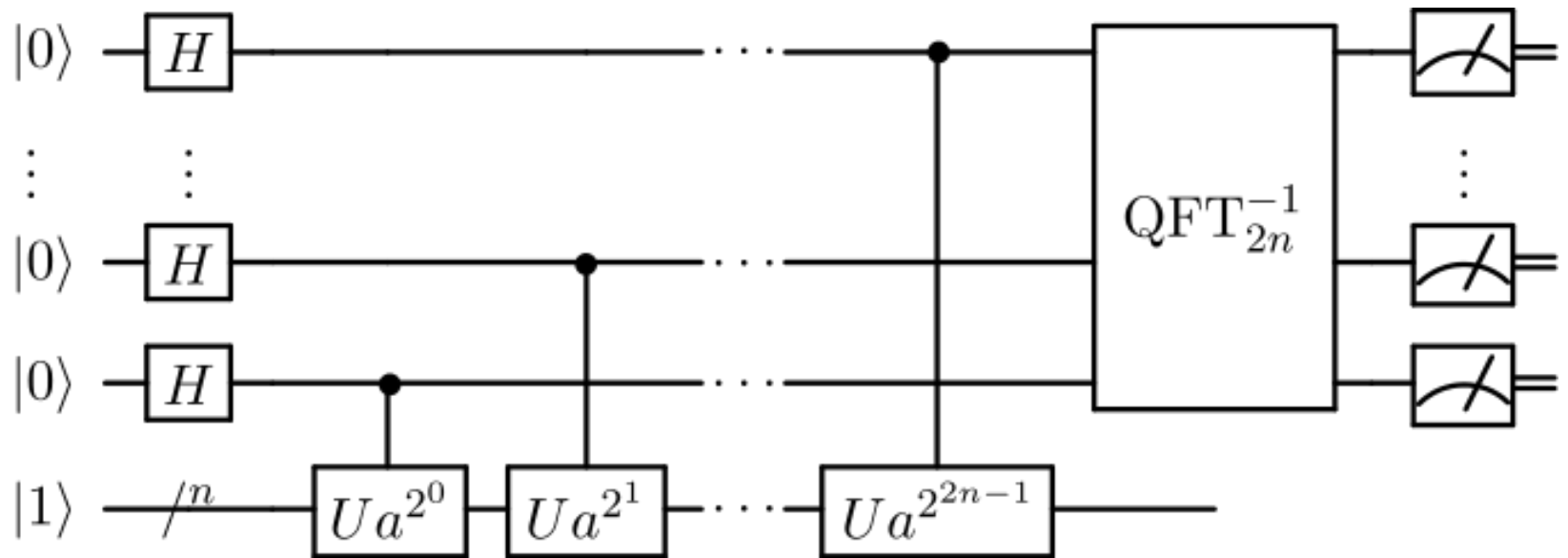
- Quantum computers seem to be good at the same kinds of things that make good trapdoor functions for asymmetric crypto (factorization, discrete log, *etc.*)
 - But not everything
 - Older schemes (*e.g.*, Merkle's signature scheme)
 - Newer schemes (*e.g.*, lattice-based)

Deutsch-Jozsa algorithm

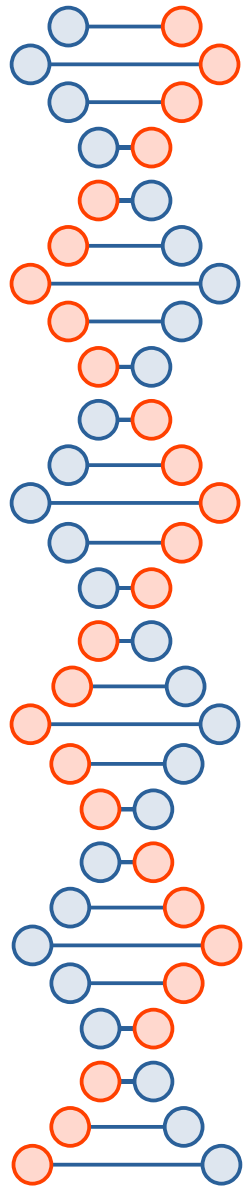


https://en.wikipedia.org/wiki/Deutsch%E2%80%93Jozsa_algorithm#/media/File:Deutsch-Jozsa-algorithm-quantum-circuit.png

Shor's algorithm

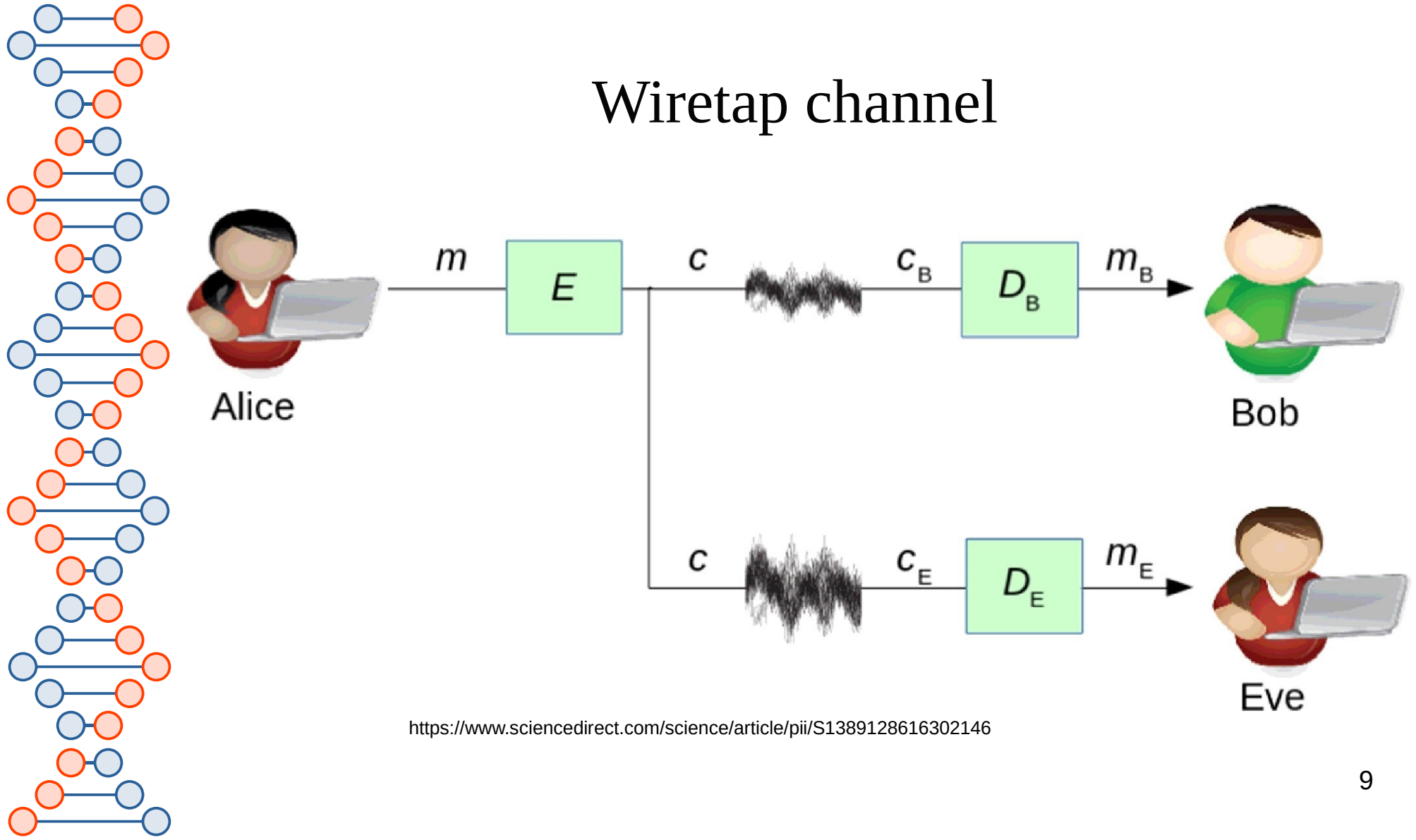


https://en.wikipedia.org/wiki/Shor%27s_algorithm#/media/File:Shor's_algorithm.svg



RSA, DH, ECDH, DSA, *etc.* all broken. Need something else instead...

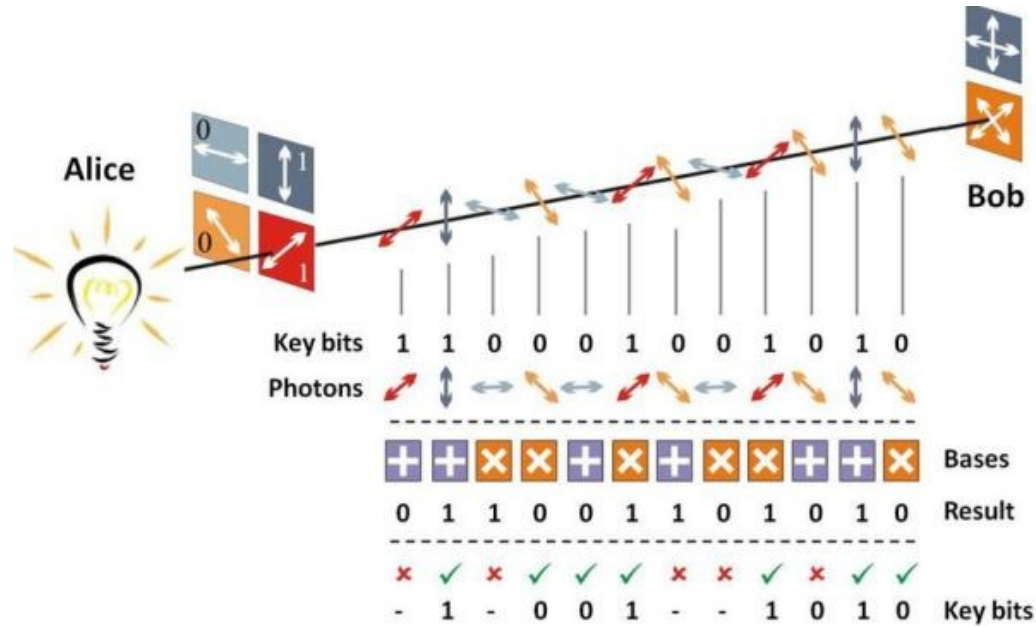
Wiretap channel



<https://www.sciencedirect.com/science/article/pii/S1389128616302146>



Quantum Key Distribution



<https://imrmedia.in/quantum-key-distribution-test-successfully-demonstrated/>



Themes

- In schemes based on information theory or physics the eavesdropper has some noise or uncertainty the receiver doesn't have
 - We'll see this in post-quantum crypto (*e.g.*, learning with errors)
- Quantum computers aren't necessarily faster at everything
 - There's usually a "trick at the end" where all the quantum information gets destroyed but the classical information measured still means something



Lamport signature (1979)

- How to sign a 256-bit message digest...
 - Generate 512 random 256-bit integers (256 pairs of them)
 - Private key
 - For all 512 generate corresponding hash
 - Public key (single use)
 - When you want to sign something, reveal one unhashed private version per pair for corresponding to the bit being 0 or 1 (*i.e.*, the first of the pair for 0, the other for 1)
 - 64 Kbits

https://en.wikipedia.org/wiki/Lamport_signature



Watch these three videos...

- https://www.youtube.com/watch?v=_C5dkUiiQnw
- <https://www.youtube.com/watch?v=QDdOoYdb748>
- <https://www.youtube.com/watch?v=K026C5YaB3A>